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70 qualitatum et velocitatum difformium, 8<sup>m</sup> de mensura et intensione in infinitum quarundam difformitatum, 9<sup>m</sup> de quodam [alio] exemplo, 10<sup>m</sup> quoddam aliud exemplum de difformitate composita ex partibus uniformibus et uniformiter difformibus, 11<sup>m</sup> de mensura et extensione in infinitum qualitatis finite seu velocitatis, 12<sup>m</sup> de infinita extensione secundum quid et mensura qualitatis finite et uniformis, 13<sup>m</sup> de infinita extensione simpliciter qualitatis finite atque difformis.

## [Capitula prime partis]

### [I.i] Capitulum primum de continuitate intensionis

Omnis res mensurabilis exceptis numeris ymaginatur ad modum quantitatis continue. Ideo oportet pro eius mensuratione ymaginari puncta, lineas et superficies, aut istorum proprietates, in quibus, ut vult Philosophus, mensura seu proportio per prius reperitur. In aliis autem cognoscitur in similitudine dum per intellectum referuntur ad ista. Etsi nichil sunt puncta indivisibilia aut linee, tamen oportet ea mathematice fingere pro rerum mensuris et earum proportionibus cognoscendis. Omnis igitur intensio successive acquisibilis ymaginanda est per lineam rectam perpendiculariter

70 qualitatum *om.* *L* / qualitatum et velocitatum: velocitatum qualitatis *C*/difformium: difformiter difformium *E* / et<sup>2</sup> *om.* *S* / intensione corr. ex extensione (*vid. cap. III.8*) / in *om.* *FM*

71 difformitatum: difformitatum difformiter difformibus (?) *A* qualitatum *E* / quodam: quorundam *F* / [alio] supplevi, cf. *III.jx.1*

71–72 quoddam...de: de quodam alio exemplo *N*

72–73 de (et *N*)...difformibus *BFMNS* *om.* *P* difformitatis composite ex partibus uniformibus *A* de difformitate *ELC*

73 et: seu *E*

74 seu: vel *N* sive *AE* / secundum: propter *EL* / quid: quam *A*

75 uniformis: uniformitatis *E* / infinita extensione simpliciter *BFM* et cf. *III.xiii.1* extensione simpliciter infinita *AELNPSC* / qualitatis<sup>2</sup> *om.* *M*

76 atque: et *N* / post difformis add. *B* Expli- ciant capitula tertie partis / post difformis add. *E* Explicit tabula capitolorum deo gratias / post difformis add. *FM* et sic est (erit *M*) finis intencionum omnium capitolorum huius libri divisi in tres partes et cetera / post difformis add. *L* Tunc sequitur prima pars

*I.i: AEBVDLNFMPCSG[J]*

1 [Capitula prime partis] *B*, *om.* *aliij MSS* prima pars tractatus [J]

2 Capitulum...intensionis *BVEG om.*

*ADLNMS[J]* de continuitate intensionis capitulum primum *F* Primum capitulum prime partis *P* Prima propositio *mg. C* 1 *mg. S*

3 Omnes res mensurabiles *NC* / ymaginatur *C*

4 mensurationem *S* mensura [J]

qualities and velocities. 8. On the measure and intension to infinity of certain difformities. 9. Another example of the same. 10. A certain other example of a difformity composed of uniform and uniformly difform parts. 11. On the measure and extension to infinity of a finite quality or velocity. 12. On the qualified infinite extension and measure of a finite and uniform quality. 13. On the absolute infinite extension of a finite and difform quality.

## Chapters of Part I

### I.i On the continuity of intensity

Every measurable thing except numbers is imagined in the manner of continuous quantity. Therefore, for the mensuration of such a thing, it is necessary that points, lines, and surfaces, or their properties, be imagined. For in them (i.e. the geometrical entities), as the Philosopher has it,<sup>1</sup> measure or ratio is initially found, while in other things it is recognized by similarity as they are being referred by the intellect to them (i.e., to geometrical entities). Although indivisible points, or lines, are nonexistent, still it is necessary to feign them mathematically for the measures of things and for the understanding of their ratios.<sup>2</sup> Therefore, every intensity which can be acquired successively ought to be imagined by a straight line perpendicular-

*I.i*

<sup>1</sup> See the Commentary, I.i, line 5.

<sup>2</sup> *Ibid.*, lines 7–9.

4–5 lineas et superficies: superficies et lineas *AP*

4 lineas: linea *N*

5 et: aut *G* / ut...Philosophus: secundum philosophum [J] / Philosophus *BVLF-MSCGD* Aristoteles *AENP*

6 seu: et *M* / per prius: proprius *GS*(?) prius *E* / autem: aut *A*

7 dum *BVFMSCG* qua *ENL* que *P* qui *A*

/ per intellectum *tr. N* post referuntur / ad ista *tr. N* post qua quod stat in loco dum / ista: illa *G* / nichil sunt: non sint *G*

8 mathematice *om.* *AP* / fingere: sumere *E*

9 proportionibus: proprietatibus et proportionibus *M* / igitur: ergo *G* aut *C*

10 ymaginanda est *tr. FM* post intensibilis in linea *xx*

11 aliquod punctum *BVFMSCG[J]* aliquot

15 caretur latitudo et intensio longitudo. Verumtamen quia extensio est manifestior et palpabilior, ut ita loquitur, et prior cognitione quo ad nos quam sit intensio, et forsitan quo ad naturam, ideo non obstantibus predictis ipsa extensio secundum communem usum loquendi attribuitur prime dimensioni, scilicet longitudini, et intensio latitudini. Et quoniam differentia 20 huiusmodi impositionis seu improprietas vocationis nichil facit ad rem sed utroque modo potest idem exprimi, volo sequi modum communem ne propter locutionem inconsuetam illa que dicam minus leviter intelligantur. Extensio igitur qualitatis in nomine dei vocetur eius longitudo et intensio 25 ipsius vocetur latitudo sive altitudo. Sed qualitercumque sit, patet ex dictis quod quidam moderni non bene vocant latitudinem qualitatis ipsam totam, sicut abusio esset per latitudinem superficie intelligere totam superficiem vel figuram. Nam quemadmodum aliquid latitudines superficierum sive figurarum inequalium sunt eae ita simili, sicut postea videbitur, multe latitudines qualitatum inequalium sunt eae aut etiam econverso.

[I.iv] Capitulum 4<sup>m</sup> de quantitate qualitatum

Cuiuslibet linearis qualitatis quantitas ymaginanda est per superficiem cuius longitude seu basis est linea in subiecto quali protracta, ut dicit precedens capitulum, et cuius latitudo seu altitudo designatur per lineam super basim predictam perpendiculariter erectam secundum quod ponit capitulum

15 intensio: intensio vocaretur *N* / Verumtamen *APCE* verum *BVFMSG* verum est tamen *LND* / quia: quod *LND* / extensio: intensio *LND*  
 16 et<sup>2</sup> om. *S* / prior: peior *G*  
 16-17 quam sit intensio om. *D*  
 17 intensio: extensio *N* / et om. *AP* / ideo: et ideo *FM* ergo *D* / ipsa om. *AP*  
 18 usum: modus *AEP*  
 19 scilicet: et i. (id est?) *V* / longitude *S*  
 19-22 Et...intelligantur om. *D*  
 19 Et: Sed *F* / quoniam: quia *AEP* / quoniam differentia *tr. L* / differentia: natura *FM*  
 20 huiusmodi: huius *B(?)VFM* / seu: vel *AEP* / proprietas *VFM* / vocationis: locationis *P*  
 21 ne: nec *L*  
 22 locutionem: modum loquendi *AP* loqua-

tionem *B* / inconsuetum *AP* / illa: ista *N* / intelligitur *N*  
 23 igitur: enim *V* ergo *S* / dei: domini *NFM*  
 23-24 eius...vocetur: ipsius *A*  
 23 eius om. *D*  
 24 ipsius: eius *LS* et *tr. S* ante intensio / ipsius *tr. G* ante latitudo / vocetur *ENPFM* om.  
*D* vocatur *L* dicatur *BVSCG* / latitudo sive altitudo: altitudo vel latitudo *P* / sive: seu *ED* vel *AP*  
 24-29 Sed...econverso om. *D*  
 24 sit om. *N* / ex dictis om. *V*  
 25 bene vocant *tr. A* quidem bene vocant *S*  
 26 esset: est *PLN* / latitudinem superficie *tr. N* / intelligere...superficie om. *S*  
 27 vel: sive *FM* aut *A* / Nam quemadmodum: non quemadmodum *S* quia sicut *AEP* quia quemadmodum *N* / aliisque: quedam *FM* / aliisque latitudines *tr. V* / sive: aut *A* vel *LP*

should be called latitude and their intensity longitude. Nevertheless, extension as it is thus spoken of is more manifest, more palpable, and prior in our cognition than is intensity.<sup>1</sup> It is perhaps also prior in nature. Therefore, notwithstanding my previous statements, this extension according to the common practice of speech is associated with the first dimension, namely longitude, and intensity with latitude. And since a difference in the application of [a name of] this sort, or an impropriety in naming, actually has no effect and the same thing can be expressed in either way, I wish [accordingly] to follow the common way. I do this so that those things which I say might not be less easily understood because of unaccustomed locution. Therefore, in the name of God let the extension of a quality be called its longitude and intensity its latitude or altitude. But however this might be, it is obvious from the things said that certain moderns do not speak in the best way when they call the whole of the quality its latitude, just as it would be an abuse [of terminology] to understand by the breadth of a surface the whole surface or figure.<sup>2</sup> For just as the breadths of some unequal surfaces or figures are equal, so, as will be seen later, many latitudes of unequal qualities are equal, or vice versa.

## I.iv On the quantity of qualities

The quantity of any linear quality is to be imagined by a surface whose length or base is a line protracted in a subject of this kind, as the preceding chapter says, and whose breadth or altitude is designated by a line erected perpendicularly on the

## I.iii

<sup>1</sup> See the Commentary, I.iii, lines 15-17.

<sup>2</sup> Ibid., lines 24-27.

I.iv: *BVAPFLSD*—collated throughout; *[MENCGJ]*—also used, but not completely, and then placed in brackets

<sup>1</sup> Capitulum... qualitatum *LBVD[CE]* om. *AS[MN]* 4<sup>m</sup> capitulum *P* De quantitate qualitatum capitulum 4<sup>m</sup> *F[G]* 4 c *mg. S* 4 *mg. A*

<sup>2</sup> linearis (linealis <sup>1</sup> *B*)...quantitas *BFS* / *[GNM]* qualitatis quantitas linealis (linearis *L[ECD]*) *ALP[CDE]* quantitas linearis qualitatis *V* / ymaginanda est *tr. AP[E]*

<sup>3</sup> seu: vel *AP[E]* / pertracta *P[M]*

<sup>3-4</sup> precedens capitulum *tr. AP[E]*

<sup>4</sup> seu *LPDF[EMNJJ]* sive *BV[CG]* sine *S*

<sup>5-6</sup> predictam... qualitatem<sup>2</sup>: aliquem *A*

<sup>5</sup> predictam: productam *LPD[EN]* / secundum... ponit: sicut dicit *P[E]* utponit *[N]*

sicut ponit *D*

corpus cuius quidem corporis ymaginati basis est superficies ipsa informata  
 qualitate prout plenius declarabitur in processu. Cum autem in corpore  
 quali infinite sint superficies [equales] et cuiuslibet earum qualitas ymaginatur  
 ut corpus, non est inconveniens, sed oportet, ymaginari unum corpus  
 secundum situm ubi aliud potest ymaginari simul, vel etiam quodlibet simul,  
 35 per penetrationem vel per mathematicam suppositionem (/superpositionem?)  
 seu simul positionem corporum sic factorum; que tamen penetratio non est  
 in re. Et quamvis qualitas superficialis ymaginetur per corpus, et non contingat  
 esse vel ymaginari quartam dimensionem, tamen qualitas corporalis  
 40 ymaginatur habere duplēcēm corporeitatem: unam veram ad extensionem  
 subiecti secundum omnem dimensionem, aliam vero solum ymaginat ab  
 intensione ipsis qualitatis infinites replicabilem secundum multitudinem  
 superficierum subiecti, cuius ymaginatio op⟨p⟩ortunitas prius tacta est et  
 in sequentibus plenius apparebit.

[I.v] Capitulum 5<sup>m</sup> de figuratione qualitatum

Omnis qualitas linearis figuratur ad modum alicuius superficiei super  
 subiectam lineam perpendiculariter erecte. Sit enim *AB* linea informata  
 qualitate [Fig. 1]. Et quoniam per precedens capitulum qualitas ista designatur  
 5 per superficiem, oportet quod ymaginetur figurata sicut superficies per  
 quam ipsa designatur vel ymaginatur. Cuius quidem superficiei altitudo  
 designat intensionem istius qualitatis. Oportet etiam quod istius superficiei

31 superficies ipsa *tr. A*  
 32 prout...declarabitur: sicut plenius patebit  
*A* sicut patebit plenius *P[E]* ut post declaratur [N] / in processu *om.* [N] / Cum:  
 nunc *F[M]* / autem: igitur *V*  
 33 sint: sum *AF[M]* / [equales] *BVAPSL*  
*[EGCN]*, sed delendum est, sicut in *F[M]*?  
 33-34 ymaginatur *F[MN]*  
 34 sed oportet *om.* *L* / sed: sed forte *F[MN]* /  
 post ymaginari *add.* *S* sit  
 35 secundum situm: sic fictum *F[N]* situm *S*  
 sic infinitum [C] / ubi...simul<sup>1</sup>; simul esse  
 ubi aliud *AP[E]* / vel: aut *A* / quodlibet:  
*E* / simul<sup>2</sup>; sive *A*  
 36 penetrationes *L[C]* / vel: seu *VF* / per  
*BSF[CGM]* *om.* *V* etiam per *AP[EN]*  
 etiam *L* / suppositionem: positionem *V*

37 positionem: possent *V* / sic *om.* *AL* / factorum  
*BVSF/MN* / situatorum *APL[E]*  
 sitorum [G] finitorum [C] / post factorum  
*add.* *L* secundum infinitatem  
 38 qualitas *om.* *L* / ymaginatur *P[N]* / et<sup>3</sup>:  
 tamen *L* et tamen [N]  
 38-39 contingat *BVFS* [MGN] contingat  
*APL* contingit [EC]  
 39 tamen *VPLS[EGC]* cum *BAF[M,?N]*  
 40 post duplēcēm add. *S* ipse  
 41-42 aliam...multitudinem *om.* *S*  
 41 vero *om.* *F[M]* / solum *VAPF[EGC]*  
 solam *BL[MN]* / solum ymaginatam *tr. A*  
 42 replicata *L*  
 44 in sequentibus: post [N] / in...apparebit:  
 postea plenius patebit *AP[E]*

as a body whose base is the surface informed with the quality. This will be more fully clarified as we go along. Moreover, since in any kind of a body there is an infinite number of equivalent<sup>4</sup> surfaces and the quality of any one of them is imagined as a body, it is not unfitting but necessary that one body be imagined to be at the same time in the place where another body—or even any other body whatever—is imagined to be. [We can think of this taking place] by penetration or by mathematical superposition<sup>5</sup> or the simultaneous placing of the bodies so imagined. However, this penetration is not real. And although a surface quality is imagined by means of a body and it does not happen that a fourth dimension exists or is imagined,<sup>6</sup> still a corporeal quality is imagined to have a double corporeity: a true one with respect to the extension of the subject in every dimension and another one that is only imagined from the intensity of this quality taken an infinite number of times and dependent upon the multitude of surfaces of the subject. The suitability of this imagined concept has been touched upon before and will be more fully apparent in what follows.

## I.v On the figuration of qualities

Every linear quality is “figured” (i.e., represented in figures) by means of a surface perpendicularly erected upon a subject line. For let *AB* be a line informed with a quality [see Fig. 1]. And since by the preceding chapter this quality is designated by a surface, it is necessary that it be imagined as “figured” by the surface by which it is designated or imagined. The latitude of this surface designates the intensity of this quality. It is necessary also that any point of this surface or figure out-

<sup>4</sup> The Latin text appears to have *superficies* *equales*. Either the *equales* ought to be deleted, or it is used with the meaning of surfaces that are equivalent or equal in thickness. One would suppose that Oresme would have conceived of them as being of infinitely small thickness, syncategorematically speaking, i.e.,

that they are thinner than any assignable quantity.

<sup>5</sup> All manuscripts except *V* (which has *positionem*) have *suppositionem*. However, *suppositionem* makes much better sense and so I have rendered it such in my translation.

<sup>6</sup> See the Commentary, I.iiv, line 39.

I.v: *BVAPFLD* [ENMCGS]

<sup>1</sup> Capitulum...qualitatum *BVLD[EC]* *om.*  
*A[M]* 5<sup>m</sup> capitulum *P* De figuratione  
 qualitatum capitulum 5<sup>m</sup> *F[G]* Capitulum  
 5<sup>m</sup> [NS] 5 c mg. S 6 mg. *A*

<sup>2</sup> lignalis *A*

<sup>3</sup> lineam *om.* [S] lignealem *A*

<sup>4</sup> quoniam: quia *AP[EN]*

<sup>6</sup> ipsa *om.* *LD[N]* / vel: aut *A* / vel ymaginatur *om.* *D*

<sup>7</sup> intensionem...qualitatis: qualitatem intensionem *A* / istius<sup>7</sup> *om.* *ALPD[N]* /  
 Oportet: et oportet *AP[E]* / etiam *om.* *AP[E]* igitur *G* / istius<sup>8</sup>: illius *AP ius[E]*  
 alicuius [S] / superficie *A*

in altitudine. Igitur erit proportionalis cuilibet quadrangulo rectangulo super  $AB$  constituto, eo quod omnes tales sunt proportionalis altitudinis quamvis tamen inequalis. Ergo per capitulum 7<sup>m</sup> ipsa qualitas est ymaginabilis per quadrangulum  $ABCD$  et similiter per quadrangulum  $ABEF$  maiorem sive etiam per minorem. Quilibet autem talis qualitas dicitur uniformis seu equalis intensionis in cunctis partibus eius.

Rursum sciendum quod aliqua qualitas est ymaginabilis per quadrangulum habentem duos rectos angulos super basim et alios inequaes, sicut per quadrangulum  $ABCD$  [Fig. 6(b)] et per omnem quadrangulum proportionalis altitudinis super basim  $AB$  constitutum sive fuerit maior sive minor, ut patet ex 7<sup>m</sup> capitulo. Quilibet autem talis qualitas dicitur uniformiter difformis terminata utrinque ad gradum, ita quod extreum intensius designatur in angulo  $C$  acuto et extreum remissius in angulo  $D$  obtuso. Superior vero linea, sicut est linea  $CD$ , dicitur linea summitatis, vel in relatione ad qualitatem potest vocari linea intensionis quia secundum varietatem ipsius variatur intensio.

### I.xi] Capitulum 11<sup>m</sup> de qualitate uniformi et difformi

Omnis itaque qualitas uniformis ymaginatur per quadrangulum rectangulum et omnis qualitas uniformiter difformis terminata ad non gradum ymaginabilis est per triangulum rectangulum. Omnis vero qualitas uniformiter difformis terminata utrinque ad gradum ymaginanda est per quadrangulum habentem rectos angulos super basim et alios inequaes. Omnis autem alia qualitas linearis dicitur difformiter difformis et est ymaginabilis per figuram aliter dispositas secundum multifariam variationem, cuius aliqui modi postea

7 altitudine: latitudine  $P$   
 7-8 cuilibet...altitudinis  $om.$   $F$  (sed habet  
 $[M]$ )  
 8 tales: scilicet tales  $L$  scilicet  $[C]$  / propor-  
 tionabilis  $V$   
 9 Ergo: igitur  $LP$  [ $ESM$ ] / 7<sup>m</sup>: 9<sup>m</sup>  $L$   
 10 similiter: simpliciter  $L$   
 10-12  $ABEF$ ...seu  $om.$   $F$  [ $M$ ]  
 11 minorem; breviorem  $V$   
 12 cunctis: omnibus  $LP$  [ $AC$ ]  
 13 sciendum  $BVF$  [ $MSG$ ] sciendum est  
 $LP$  [ $EANC$ ] / est ymaginabilis  $tr.$   $FP$   
 $[EM]$   
 14 rectos: equales  $P$  [ $A$ ] / rectos angulos  $tr.$   
 $V$  [ $N$ ]  
 15-16 proportionabilis  $V$

16-17 sive!...dicitur  $om.$   $F$  [ $M$ ]  
 16 minor: brevior  $V$   
 17 ex 7<sup>m</sup>  $BV$  [ $ESG$ ] in 7<sup>m</sup> [ $N$ ] 9<sup>m</sup>  $LP$  [ $A$ ] in  
 $[C]$   
 18 terminata utrinque  $tr.$   $LP$  / utrinque  $B/C$   
 utrique  $LP$  [ $G$ ] ubique  $V$  utriusque  $F$  [ $M$ ]  
 utrimeque  $[ES]$  utrobique  $[A]$  uterque  $[N]$   
 / ad: per  $L$  [ $N$ ]  
 19 C: DC  $P$  de CDC  $[A]$   
 20 sicut  $om.$   $[M]$  / est linea  $om.$   $F$  / linea<sup>2</sup>  
 $BV$  [ $MSG$ ]  $om.$   $LP$  [ $EANC$ ]  
 21 quia: que  $P$   
 22 intensio: 7<sup>a</sup>  $F$  intensio 7<sup>a</sup>  $[M]$   
 I.xi:  $BVPFL$   
 1 Capitulum...difformi  $om.$   $[MAS]$  capitu-

Therefore, it will be proportional to any rectangle constructed on  $AB$ , because all such rectangles are of proportional, although unequal, altitude. Therefore, by chapter seven, this quality is imaginable by rectangle  $ABCD$  and similarly by rectangle  $ABEF$  which is greater and also by one that is less. Moreover, any such quality is said to be "uniform" or "of equal intensity" in all of its parts.

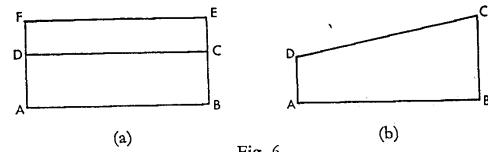


Fig. 6 Figures in MSS *BLSCG*. Letters  $C$  and  $D$  in figure (a) are interchanged in MS *L*.

Again it ought to be known that some quality is imaginable by a quadrangle having two right angles on the base and the other two angles unequal, e.g., by quadrangle  $ABCD$  [see Fig. 6(b)] and by every quadrangle constructed on base  $AB$  which is of proportional altitude, whether it be greater or less, as is clear in chapter seven. Moreover, any such quality is spoken of as "uniformly difform terminated in both extremes at some degree," so that the more intense extreme is designated in the acute angle  $C$  and the more remiss in the obtuse angle  $D$ . The superior line, e.g., line  $CD$ , is called "the line of summit," or in relation to quality it can be called "the line of intensity" because the intensity varies according to its variation

### I.xi On uniform and difform quality

And so every uniform quality is imagined by a rectangle and every quality uniformly difform terminated at no degree is imaginable by a right triangle. Further, to every quality uniformly difform terminated in both extremes at some degree is to be imagined by a quadrangle having right angles on its base and the other two angles unequal. Now every other linear quality is said to be "difformly difform" and is imaginable by means of figures otherwise disposed according to manifold variation. Some modes of the "difformly difform" will be examined later. The

lum 11<sup>m</sup> [ $N$ ] 11 mg.  $[SA]$  / Capitulum  
 11<sup>m</sup>  $tr.$   $P$   
 2 itaque: igitur  $P$  [ $A$ ]  
 2-3 rectangulum  $om.$   $L$   
 4 est  $om.$   $F$  [ $MAC$ ] / Omnis vero: et omnis  
 $F$  [ $M$ ] omnis ergo  $[C]$   
 4-5 uniformiter difformis  $om.$   $L$  [ $N$ ]  
 5 utrinque ad  $BF$   $tr.$   $[N]$  utrinque ad  $P$  [ $G$ ]

utrimque ad  $[SE]$  utriusque ad  $[A]$  utrumque  
 ad  $[C]$  utramque ad  $V$  ad utrumque  
 $L$  [ $M$ ] / gradum: non gradum  $B$   
 7 qualitas linearis: linealis qualitas  $P$  linearis  
 qualitas  $[E]$  lignealis qualitas  $[A]$  / yma-  
 ginabilis: ymaginanda  $LP$  [ $EANC$ ]  
 8 variationem: varietatem  $P$

coniungatur basi, qualitas sive difformitas terminatur utrinque ad gradum. Et quoniam talis linea non potest coniungi basi in utroque extremo, quia ipsa est recta et basis recta et sic esset linea una, inde patet quod non potest esse aliqua qualitas uniformiter difformis terminata utrinque ad non gradum.  
 Si vero linea intensionis sive summitatis fuerit curva aut ex multis lineis composita et non una, tunc qualitas per illam figuram ymaginabilis erit difformiter difformis et potest esse quod terminatur utrinque ad gradum vel utrinque ad non gradum vel ad gradum in uno extenso et ad non gradum in altero.

[I.xiv] Capitulum 14<sup>m</sup> de simplici difformitate difformi

Difformis difformitatis de qua nunc agitur duo sunt modi; quedam enim est simplex et alia est composita. Et primo dicendum est de simplici. Est igitur simplex difformitas difformis que designabilis est per figuram cuius linea summitatis sive linea intensionis est una, non composita ex pluribus. Oportet igitur quod sit linea curva; quia si foret recta, iam esset uniformitas simpliciter aut uniformis difformitas, ut patet ex capitulo precedenti. Necesse est etiam quod eius curvitas non attingat ad circuli portionem maiorem semicirculo ita ut angulus super basim sit maior recto, ut patuit ex 4<sup>o</sup> (15<sup>o</sup>) capitulo. Potest tamen fieri ut angulus super basim sit minor recto etiam quantumlibet.

Sit igitur, gratia exempli, linea *AB*, cuius qualitas sit designabilis per semicirculum *ACB* [Fig. 10], quod est possibile, ut patet ex 7<sup>o</sup> capitulo. Nunc itaque dico quod eadem qualitas linee *AB* est ymaginabilis seu designabilis per figuram maioris altitudinis ac etiam minoris isto semicirculo etiam quantumlibet. Protrahatur enim linea *CD* perpendicularis super centrum *D*

11 terminatur tr. *P post gradum / utrinque B utrique P utrobique VL[EAN] ad utrumque F[MG] utrimque [S] / ad: ad non P[A]*

12-14 Et...gradum om. *F[M]*

12 non om. *L / quia: quoniam L[A] nam [E]*

13 linea: linea recta *L*

14 terminata utrinque: utrobique terminata usque *P[E]* terminata usque *L* terminata utrobique *[AC]* / utrinque om. *BLF[N]* utrique *[G]* utrimque *[S]* utrobique *VP[EAC]*

17 difformis: difformis terminata *V / esse...* terminatur; etiam terminari *L* etiam quod terminari *[E] / utrinque<sup>1,2</sup> BP[N] utro-*

bique *V[C]* utriusque *F[MA]* utrinque *[SE]* utriusque *[G]* / utrinque...utrinque om. *L*

17-18 vel...gradum<sup>3</sup> om. *[M]*

18 altero *E a<sup>o</sup> B[AN]* alio *FLV[SPMCG]*

I.xiv: *BVLPC*

1 Capitulum...difformi [om. *MANS*] 14  
mg. *[SA]* / Capitulum 14<sup>m</sup> tr. *F post dif-*  
*forni*

2 ago *F[M]* / quedam bis *B* quidem *[A]*

2-3 enim est tr. *P autem est [A]*

3 est<sup>4</sup> om. *[C]* / et om. *LP[EG]* / alia: quedam *F[MN]* aliaque *[G]* / est<sup>2</sup> *VLP[ACS]* om. *BP[EMNG]*

and if it is joined to the base in neither extreme the quality or difformity is terminated in both extremes at [some] degree. And since such a line cannot be joined to the base in both extremes—for it is a straight line and thus would form a single line with the base which also is a straight line—it is clear that there cannot be a quality uniformly difform terminated in both extremes at no degree. Further, if the line of intensity or summit line is a curve or is composed of several lines rather than one, then the quality imaginable by that figure will be difformly difform, and it can be that it is terminated in both extremes at some degree, or in both extremes at no degree, or at some degree in one extreme and at no degree in the other.

## I.xiv On simple difform difformity

We now treat of difform difformity; there are two modes of such difformity: simple and composite. We must first talk of the simple mode. Simple difform difformity is that which can be designated by a figure whose line of summit or line of intensity is a single line, i.e. not composed of several lines. It is necessary, therefore, that the line be a curve; because if it were straight, then it would be simply a uniformity or uniform difformity, as is clear from the preceding chapter. Furthermore, it is necessary that the curvature of the summit line does not attain that of a circular segment greater than a semicircle so that the angle<sup>1</sup> on the base is greater than a right angle, as was clear in chapter five.<sup>2</sup> However, it can happen that the angle on the base is less than a right angle by any amount you please.

Therefore, for example, let there be line *AB*, whose quality can be designated by semicirculum *ACB* [see Fig. 10]. This is possible, as is evident from chapter seven. And so I now say that the same quality of line *AB* is imaginable or can be designated by a figure having an altitude greater or less than that of the semicircle by any amount you please.<sup>3</sup> For let line *CD* be drawn as a perpendicular to center *D* and

## I.xiv

<sup>1</sup> In this case the angle would be a mixed angle composed of the curve and the straight base line.

<sup>2</sup> All the manuscripts have “chapter 4,” but this is a clear reference to the penultimate sentence in I.v.

<sup>3</sup> See the Commentary, Ixiv, lines 14-34.

5 sive: seu *BF[EMC]* / pluribus: partibus *L* partibus pluribus *[N]*

6 quia: que *P[EA]* / foret: esset linea *F[M]* foret linea *[E]* esset *[C]* / esset: foret *P[E]* foret *[A]*

9 ut<sup>1</sup> *BVF[ACGS]* quod *LP[EMN]* / patet *L / ex om. P[A]* / 4<sup>o</sup> capitulo *BVF[MS]* tr. *LP[EANGC]*

10 etiam: et *P[G]*

13 *ACB BV[FM] ABC PL[AENGCS]* / patuit *V / 7<sup>o</sup> capitulo tr. P[E] 4<sup>o</sup> capitulo F[M] capitulo alio [A]*

14 linea *B*

15 maioris om. *L / ac: aut P[A] / ac etiam om. L*

16 supra *LP[M]*

Deo, de quo scriptum est in libro Danielis quod “ipse revelat profunda et abscondita, et novit in tenebris constituta.”

Incipit secunda pars  
huius tractatus de difformitate  
successivorum

[II.i] Capitulum primum de duplice difformitate motus

5 Omnis motus successivus subiecti divisibilis habet partes et est divisibilis uno modo secundum divisionem et extensionem seu continuitatem mobilis, alio modo secundum divisibilitatem et durationem seu continuitatem temporis, tertio modo saltem ymaginative secundum gradus et intensionem velocitatis. A prima autem continuitate dicitur motus magnus vel parvus, a secunda brevis aut longus, a tercia velox aut tardus. Habet itaque motus duplē extensionem, unam subiectivam et aliam temporalem, et habet unam intensionem. Due autem extensiones possunt ymaginari quodam modo orthogonaliter seinvicem ad modum crucis intersecare, ita quod extensio durationis diceretur longitudo et extensio subiectiva vocaretur latitudo, intensio vero posset vocari altitudo ipsius motus seu velocitatis. Sed si iuxta premissa in 3º capitulo prime partis intensio velocitatis appellaretur eius latitudo, tunc utraque extensionum ad intensionem comparata poterit dici longitudo et sic velocitas habebit duplē longitudinem sicut habet duplē extensionem, et in utraque istarum extensionum potest intensio velocitatis multipliciter variari. Et quoniam difformitas oritur ex eo

28 post Danielis add. [G] 3º (I) capitulo

28-29 de ipse...constitute scr. mg. B in (?)  
Danl' 2 et mg. A Daniel 28 (I) / et abs-  
condita om. B [P]

29 et om. L / et...constitute om. [C] sed add.  
et sic est finis illius capituli et per conse-  
quens totius tractatus / post constituta add.  
[E] Explicit prima pars huius tractatus  
deo gratias et add. [PFM] Explicit prima  
pars huius operis et [A] explicit prima  
pars et [N] Et sic finitur prima pars prin-

cipalis et [G] Explicit prima pars de inten-  
sione qualitatum

*Tit. et II. i: BVL*

1-3 Incipit (om. L)...successivorum BL[A]  
om. V[N] Incipit secunda [FMP] Secun-  
da pars de figuratione et potentia successi-  
vorum [G] Secunda pars particularis mg.  
[C] Incipit pars secunda [E] secunda pars  
mg. [S] Secunda pars [J]  
4 duplē om. L

or by good or bad angels, or immediately by God, of whom it has been written in the book of Daniel<sup>2</sup> that “He revealeth deep and hidden things and knoweth what is in darkness.”

Here begins the second part  
of this tract and it treats of the difformity  
of successive things

II.i On the double difformity of motion

Every successive motion of a divisible subject has parts and is divisible in one way according to the division and extension or continuity of the mobile, in another way according to the divisibility and duration or continuity of time, and in a third way—at least in imagination—according to the degree and intensity of velocity. From its first continuity motion is said to be “great” or “small”; from its second, “short” or “long,” and from its third, “swift” or “slow.” And so motion has two extensions, one that pertains to the subject and the other that pertains to time, and one intensity. Now the two extensions can be imagined in a certain way as mutually intersecting at right angles in the manner of a cross,<sup>1</sup> so that the extension of duration ought to be said to be “longitude” and the extension in subject ought to be called “latitude,” while the intensity could be called the “altitude” of this motion or velocity. But according to what was premised in the third chapter of the first part, if intensity of velocity were to be called its “latitude,” then each of the extensions in relationship to intensity could be called “longitude,” and so velocity will have a double longitude just as it has a double extension, and in each of these extensions the intensity of velocity can be varied in multiple ways. And since dif-

<sup>2</sup> Daniel 2:22.

II.i

<sup>1</sup> See the Commentary, II.i, lines 12-13.

5 subiecti: sive L

6 extensionem et divisionem L / continua-  
tionem V

7 et: temporis et L

7-8 temporis: eiusdem L

10 aut<sup>1,2</sup>: vel L

12 Due: que (?) L

13 orthogonaliter B[SG] / se: seu L / seinvic-  
em fr. V post crucis

15 posset BV[AFCM] potest L[ENSG]  
possit [P]

16 intensio: in tempore [PFM]

[II.iii] Capitulum 3<sup>m</sup> de quantitate intensionis velocitatis

Cum utraque uniformitas motus primo capitulo posita consistat in intensionis equalitate et utraque difformitas ex inequalitate proveniat premitendum est penes quid attendatur quantitas gradualis intensionis ipsius velocitatis. Verumtamen circa velocitatem tria sibi invicem propinqua possunt considerari. Unum est quantitas ipsius velocitatis totalis pensatis intensione et extensione, et de hoc dicetur in tertia parte huius tractatus que erit de mensuris qualitatum et velocitatum. Aliud quoque potest ibi considerari, scilicet denominatio qua subiectum dicitur tale fieri velocius aut tardius, de quo etiam dicetur in capitulo sequenti. Tertium est ipsa gradualis intensio que facit ad istud propositum, et de qua nunc dicendum est. Dico ergo quod universaliter ille gradus velocitatis est simpliciter intensionis sive maior quo in tempore equali plus acquiritur vel deperditur de illa perfectione secundum quam fit motus. Verbi gratia, in motu locali ille gradus velocitatis est maior et intensionis quo plus pertransiretur de spatio vel de distantia, et in alteratione similiter ille gradus velocitatis est maior quo plus acquireretur vel deperderetur de intensione qualitatis, et ita in augmentatione quo plus acquireretur de quantitate et in diminutione quo plus deperderetur de quantitate vel de extensione, et ita generaliter ubicunque reperiatur motus.

[II.iv] Capitulum 4<sup>m</sup> de diversis modis velocitatis

Non est pretermittendum quod idem motus vel fluxus multis nominibus diversimode connonantibus appellatur et secundum hoc velocitas denominans diversimode attenditur sive mensuratur, ita quod quantitas intensionis gradualis multis modis assignatur, quibus tamen convenit descriptio prius dicta in capitulo precedenti.

Verbi gratia, primo in motu circulari mobile dicitur moveri et dicitur

*II.iii: BVL*

- 1 intensionis velocitatis *tr. L[E]*
- 2 primo: ex primo *L[EN]* / posita *om. L[E]*
- 3 quoque: etiam *L*
- 4 aut: vel *L[G]* sive *A*
- 5 istud *V[ESN]* illud *L[PM]* <sup>i</sup><sub>4</sub> *B[AFCG]*  
/ et *B[AFMPCSG]* *om. LV[EN]* / qua:  
quod *L* / dicenda *B* / ergo *BV[APCGM]*  
igitur *L[ENFS]*
- 6 quod universaliter *tr. L[EN]*
- 7 universaliter *tr. [FMP]* *ante est* / quo: alio

[*FMP*]

- 8 velocitatis: motus vel velocitatis [*FMP*]
- 9 14-15 maior et intensionis *B[SG]* maior (quo plus acquireretur aut deperderetur de intensione) et intensionis [*A*] maior vel intensionis [*FMP*] maior sive intensionis [*C*] intensionis et maior *L[EN]* intensionis sive maior *V*
- 10 16 velocitatis *om. V*
- 11 17 de: in *B*
- 12 18 acquireretur *om. V*
- 13 19 reperiatur *BV[AFSG]* reperiatur [*ENMP*]

## II.iii On the quantity of the intensity of velocity

Since each uniformity of motion posited in the first chapter consists in equality of intensity and each difformity arises from inequality [of intensity] we ought to set out first [the measure of gradual intensity, i.e. we ought to specify] with what the gradual intensity of the velocity is measured. However, in the matter of velocity three closely related ideas can be considered. One is the total quantity of the velocity taking into account both intensity and extension. I shall speak of this in the third part of this tract, which will be concerned with the measures of qualities and velocities. Another thing to be considered in connection with velocity is the denomination in terms of which a subject is said to become such a kind more quickly or more slowly. I shall also speak of this in the following chapter. Third, there is the gradual intensity [of velocity]. This is the subject which must now be considered. Therefore, I say universally that that degree of velocity is absolutely more intense or greater by means of which in an equal time more is acquired or lost, of that perfection according to which the motion takes place.<sup>1</sup> For example, in local motion that degree of velocity is greater and more intense by means of which more space or distance would<sup>2</sup> be traversed. In alteration, similarly, that degree of velocity is greater by means of which more intensity of quality would be acquired or lost; and so in augmentation, by means of which more quantity is acquired, and in diminution, by means of which more quantity or extension is lost. And so generally [our definition would hold] wherever motion would be found.

## II.iv On diverse ways of [considering] velocity

We must not overlook the fact that the same motion or flux is called by many names that connote a variety of things, and, according to the denomination, velocity is attended or measured in a variety of ways, so that the quantity of gradual intensity is assigned in diverse ways; with which, however, the definition stated earlier in the preceding chapter is in accord.

For example, first, in circular motion a mobile is said "to be moved" and it is

*II.iii*

<sup>1</sup> See the Commentary, II.iii, lines 11-14.

<sup>2</sup> *Ibid.*, line 15.

*CJ* reperiuntur *L*

*II.iv: BVL*

- 1 idem: idem est *L*
- 2-3 nominibus diversimode *tr. LV*

<sup>3-4</sup> denominans: denominata *L[E]* denominata nominans [*N*]

<sup>4</sup> post quod add. *B* quantitas intensionis sive mensuratur ita quod

<sup>7</sup> movere *V*

motu sed tamen reducibles ad premissas. In motu enim quandoque est successio secundum inceptionem. Verbi gratia, in motu locali possibile est quod aliquod mobile totum simul incipiat moveri et possibile est quod incipiat moveri pars post partem, sicut si punctus *D* [Fig. 15] ymaginetur fluere super mobile *AB* ita quod pars ipsius mobilis *AB* pertransita a puncto *D* moveatur et pars nundum pertransita quiescat donec pertranseat a punto *D*, sicut esset de virga plicabili que sic inciperet moveri. Hoc autem precise habet locum in motu alterationis ubi reperitur successio secundum partes quantitativas subiecti ac etiam in generatione forme substantialis materialis; in qua generatione est successio secundum partes quantitativas sive secundum extensionem, non tamen secundum partes graduales et intensio[n]em, sicut est in generatione ignis. Huiusmodi vero successio assimilatur quadam modo motui locali, sicut patet in exemplo nunc posito de motu puncti *D*, et quadam modo assimilatur augmentationi secundum hoc quod continue plus et plus sive maior et maior portio de subiecto movetur, vel quod plus est generatum de forma. Et omnis successio que in hoc reperitur aut est secundum partes subiecti aut secundum partes temporis aut secundum velocitatem istius successionis secundum quod in exemplo posito punctus *D* ymaginaretur moveri velocius aut tardius, et sic totum reducitur ad tres divisibilitates in primo capitulo assignatas. Propter quod omnis uniformitas sive difformitas que posset in hac successione inveniri reducenda est et continetur sub duobus generibus uniformitatis et difformitatis in primo capitulo iam positis.

Adhuc autem potest ymaginari alia successio, omnis enim velocitas est intensibilis et remissibilis. Eius vero continua intensio vocatur velocitatio et hec quidem velocitatio seu augmentatio velocitatis potest fieri velocius aut tardius. Unde quandoque contingit quod velocitas intenditur et velocitatio remittitur, quandoque vero utraque simul intenditur. Et similiter huiusmodi velocitatio aliquando fit uniformiter et aliquando difformiter et diversimode. Sed quoniam omnis divisibilitas sive successio que in huiusmodi velocitatione reperitur est aut secundum partes subiecti aut secundum partes tem-

3 assignatam: ymaginatam *V* / possunt  
*L*[*N*] / ymaginari *BL*[*AEP CNSG*] assi-  
gnari *V*[*M*] assignari aut ymaginari [*F*]  
4 premissa *V*  
5 inceptionem: interruptionem *L*[*E*]  
7 si punctus: penes [*FMPC*]  
8 pertransita: pertranseat [*FMPC*]  
9 nondum *V*  
11 precise *L*[*ENFC*] precipe *V*[*AG*] pre-  
scise [*M*] precipe *B*[*PS*]  
14 sive: materie sive *L*[*E*]  
18 et<sup>2</sup> *L*[*AESG*] ac *BV* sive [*FPC*]

19 est generatum *BV*[*AS*] tr. [*FMP*] gene-  
ratur *L*[*EN*]  
21 istius: ipsius *L* / posito *om.* *L*  
22 ymaginatur *L*  
23 tres: tres divisiones vel *L*  
24 potest *L* / in... successione *om.* *L*  
26 iam *om.* *L*  
27 alia: una alia *L* / velocitas: successio *V*  
28 continua *om.* *V*  
31 quandoque: et quandoque *V* / vero *om.* *V*  
32 aliquando: quandoque *L* / et *om.* *V*  
33 omnis *om.* *L* / divisibilitas: diversitas *L* /

these however are reducible to those premised. For sometimes in motion there is succession according to inception. For example, in local motion it is possible that the whole of some body begins to be moved at the same time, but it is possible [at another time] that one part begins to be moved after another. A case in point is if point *d* [see Fig. 15] is imagined to flow over mobile *AB* so that the part of mobile

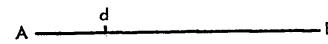


Fig. 15  
Figure in MS B.

*AB* traversed by point *d* is moved and the part not yet traversed remains at rest until traversed by point *d*, as in a pliable rod which would begin to be moved in this way. But this is precisely what happens in the motion of alteration where succession is found according to quantitative parts of the subject and even in the generation of substantial, material form. In such generation there is succession according to quantitative parts, or according to extension, but not however according to gradual parts and intensity. An example is in the generation of fire. Succession of this kind is assimilated in a certain way to local motion, as is evident in the example just posited of the motion of point *d*, and it is [also] assimilated in a certain way to augmentation since there [i.e., in augmentation] continually more and more, or a greater and greater portion, of the subject is moved or more form is generated. But every succession which is found in this [type] is (1) according to parts of the subject, or (2) according to parts of the time, or (3) according to the velocity of the succession—as, in the example posited, point *d* would be imagined to be moved more quickly or more slowly. And everything thus is reduced to the divisions specified in the first chapter. Accordingly, every uniformity or difformity which could be found in this kind of succession is to be reduced to, and is contained in, the two kinds of uniformity and difformity already posited in the first chapter.

There can be imagined one further succession, for every velocity is capable of being increased in intensity and decreased in intensity. Now its continuous increase in intensity is called acceleration, and indeed this acceleration or augmentation of velocity can take place more quickly or more slowly.<sup>1</sup> Whence it sometimes happens that velocity is increasing and acceleration is decreasing, while sometimes both are simultaneously increasing. Similarly acceleration of this sort sometimes takes place uniformly and sometimes non-uniformly and in diverse ways. But since every divisibility or succession which is found in acceleration of this sort is according to parts of the subject, or according to parts of the time, or ac-

II.v

<sup>1</sup> See the Commentary, II.v, lines 27–32.

que: que est *L*

34–35: temporis: corporis [*FMP*]

<sup>40</sup> cordias domini in eternum cantabunt, quo canticum in gloriam gratiae Christi [...] nichil erit profecto illi iocundius civitati."

Incipit tertia pars  
de acquisitione et mensura qualitatum  
et velocitatum

[III.i] Capitulum primum: per quid ymaginanda est  
acquisitio qualitatis

Duplici modo potest contingere successio in acquisitione qualitatis, scilicet secundum extensionem et secundum intensionem, sicut superius fuit dictum capitulo 4<sup>o</sup> partis secunde. Acquisitio itaque extensiva qualitatis linearis ymaginanda est per motum puncti fluentis super ipsam lineam subiectivam, ita quod pars pertransita sit qualificata et pars nundum pertransita non qualificata. Sicut si punctus *c* moveretur super lineam *AB* et quidquid esset ab eo pertransitum esset album et quidquid nundum esset pertransitum nundum esset album [Fig. 18(a)]. Acquisitio autem extensiva qualitatis superficialis ymaginanda est per motum linee dividentis partem superficiei

40 Christi om. *L*

41 profecto *B[AFMSG]* text. *Aug.* perfecto *L[VPC]* perfectius *[N]* / illi iocundius *tr. L[N]* iocundius *[A]* / post civitatem add. *[PM]* et sic est finis istius. Explicit secunda pars huius tractatus, et add. *[F]* et sic est finis, et add. *[G]* Explicit secunda pars, et add. *[A]* Amen. Explicit secunda pars huius tractatus, et add. *[N]* Explicit secunda pars et add. *L* Sequitur (!) pars huius tractatus, et add. *[S]* et sic explicit pars secunda

*Tit. et III.i: BL*

1-3 Incipit...velocitatum *mg.* *BL[ANG]* (except for the variants in *BAL* below) *om.* *[VP]* Incipit tertia etc. *[M]* Incipit 2<sup>a</sup> (!) pars que est de configuratione et potentia qualitatum successivorum *[F]* Tertia pars

Part III, Chapter i

of God in eternity ... certainly there will be no greater joy in that city than this song to the glory of the grace of Christ."<sup>5</sup>

Here begins the third part  
[of this treatise]: On the Acquisition and Measure  
of Qualities and Velocities

III.i How the acquisition of quality is to be imagined

Succession in the acquisition of quality can take place in two ways; (1) according to extension, (2) according to intensity, as was stated in the fourth chapter of the second part. And so extensive acquisition of a linear quality ought to be imagined by the motion of a point flowing over the subject line in such a way that the part

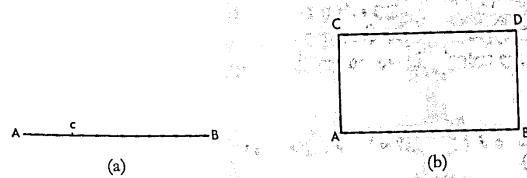


Fig. 18  
Figure (a) in MSS *BG*. Figure (b) in MSS *SJGL*. MS *L* merely has two parallel lines *AB* and *CD* close together.

traversed has received the quality and the part not yet traversed has not received the quality. An example of this occurs if point *c* were moved over line *AB* so that any part traversed by it would be white and any part not yet traversed would not yet be white [see Fig. 18(a)]. Further the extensive acquisition of a surface quality ought to be imagined by the motion of a line dividing that part of the surface that

<sup>5</sup> *De civitate Dei*, XXII, 30 (ed. of Dombart, Vol. 2, 633-34): "Alioquin si se fuisse miseris nesciuri sunt, quo modo, sicut ait psalmus, iucundus civitati." Augustine is referring to *mistericordias Domini in aeternum cantabant?* Quo *Psalmi 88:2*.

ymaginetur ens successivum. Unde in Ysaia dicitur, "erit lux lune sicut lux solis, et lux solis erit septempliciter sicut lux septem dierum," quia videlicet lux unius diei septempliciter intensa equalis est luci que per septem dierum spatium extenderetur.

[III.vii] Capitulum 7<sup>m</sup> de mensura qualitatum et velocitatum difformium

Omnis qualitas, si fuerit uniformiter difformis, ipsa est tanta quanta foret qualitas eiusdem subiecti vel equalis uniformis secundum gradum puncti mediū eiusdem subiecti; et hoc intelligo si qualitas fuerit linearis. Et si fuerit superficialis, secundum gradum linee mediae; si vero fuerit corporalis, secundum gradum medie superficie, semper conformiter intelligendo. Istud ostenditur primo de linearī. Sit igitur una qualitas ymaginabilis per triangulum  $ABC$  que est uniformiter difformis terminata ad non gradum in punto  $B$  [Fig. 21(a)]; et sit  $D$  punctus medius linee subiective, cuius quidem puncti gradus vel intensio ymaginatur per lineam  $DE$ . Igitur qualitas que es-  
set uniformis per totum subiectum secundum gradum  $DE$  ymaginabilis est per quadrangulum  $AFGB$ , ut patet per 10<sup>m</sup> capitulum prime partis. Constat autem per 26<sup>am</sup> primi Euclidis quod duo parvi trianguli  $EFC$  et  $EGB$  sunt

<sup>28</sup> ens  $B[VAFMPC]$  esse  $L[SG]$  esse ens  $[N]$   
<sup>29-30</sup> videlicet lux  $tr. L$  lux  $[N]$   
<sup>31</sup> extenditur  $L[S]$

III.vii: BL  
3-4 ipsa...uniformis om. [FMP]  
5 si...linearis: qualitate linearī  $B$

7 media superficie  $tr. L[NS]$  superficie  $[V]$   
/ semper: secundum hoc  $L$   
8 ostenditur primo  $tr. L[G]$  ostenditur  
[FMP]  
11-12 esset  $B[VASG]$  est  $L[NFMP]$   
13-14 Constat autem  $B[VSG]$  constatque  
 $L[N]$  constat et [FMP]  
14 EFC: EFG  $B[V]$

Part III, Chapter 7

if it is imagined to be a successive entity. Whence it is said in Isaías:<sup>3</sup> "And the light of the moon shall be as the light of the sun, and the light of the sun shall be sevenfold as the light of seven days," for evidently the light of one day increased intensively by sevenfold is as the light which would be extended through a space of seven days.

III.vii On the measure of difform qualities and velocities

Every quality, if it is uniformly difform, is of the same quantity as would be the quality of the same or equal subject that is uniform according to the degree of the middle point of the same subject.<sup>4</sup> I understand this to hold if the quality is linear. If it is a surface quality, [then its quantity is equal to that of a quality of the same subject which is uniform] according to the degree of the middle line; if corporeal, according to the degree of the middle surface, always understanding [these concepts] in a conformable way. This will be demonstrated first for a linear quality. Hence let there be a quality imaginable by  $\triangle ABC$ , the quality being uniformly difform and terminated at no degree in point  $B$  [see Fig. 21(a)]. And let  $D$  be the middle point of the subject line. The degree of this point, or its intensity, is imag-

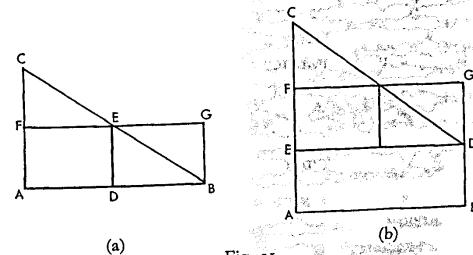


Fig. 21  
Figures in *BLSJG*. Figures are rotated through 90° in MS *G*. In figure (b) in MS *L*, there is no center perpendicular. In MS *J*, line  $ED$  is missing and the center perpendicular is marked  $KH$ . Both figures are reversed in MS *J*.

ined by line  $DE$ . Therefore, the quality which would be uniform throughout the whole subject at degree  $DE$  is imaginable by rectangle  $AFGB$ , as is evident by the tenth chapter of the first part. Therefore, it is evident by the 26th [proposition] of [Book] I of the *Elements* of Euclid<sup>2</sup> that the two small triangles  $EFC$  and  $EGB$

III.vii

<sup>1</sup> See the Commentary, III.vii, lines 3-5.

<sup>2</sup> *Ibid.*, line 14.

<sup>3</sup> *Isaias* 30:26.